A preliminary report of the space group of a copper dimethylglyoxime crystal has recently appeared (Bua $\&$ Schiavinato, 1951 ). The space group is reported to be $P 2_{1} / n$ with four molecules in the unit cell. It would not be necessary, then, to have a centro-symmetrical molecule in the copper dimethylglyoxime structure.

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# The Molecular Structure of 1,1,2,2-Tetramethylcyclopropane* 

By H. P. Lemaire $\dagger$ and R. L. Livingston<br>Department of Chemistry and Purdue Research Foundation, Purdue University, Lafayette, Indiana, U.S.A.

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The structure of 1,1,2,2-tetramethylcyclopropane has been investigated by electron diffraction. The results indicate an average $\mathrm{C}-\mathrm{C}$ bond distance of $1.52 \pm 0.03 \AA$ and an external angle $\left(\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}\right)$ of $114 \pm 6^{\circ}$.

## Introduction

The two main points of interest in connection with the structure of cyclopropane or of its derivatives are the $\mathrm{C}-\mathrm{C}$ bond distance in the ring and the value of the external angle (the $\mathrm{H}-\mathrm{C}-\mathrm{H}$ angle in cyclopropane and the corresponding angle in its derivatives). There is evidence that the $\mathrm{C}-\mathrm{C}$ distance is shorter than in most hydrocarbons and that the external angle is greater than tetrahedral. In cyclopropane Pauling \& Brockway (1937) have given $1.53 \pm 0.03 \AA$ and $109.5^{\circ}$

[^0]for these parameters; more recently Bastiansen \& Hassel (1946) found values of $1.535 \AA$ and $118 \cdot 2 \pm 2^{\circ}$. In 1,1-dichlorocyclopropane O'Gorman \& Schomaker (1946) have found a C-C distance of $1.52 \pm 0.02 \AA$ and a $\mathrm{Cl}-\mathrm{C}-\mathrm{Cl}$ angle of $112 \pm 4^{\circ}$. Smith (1941), from infra-red data, arrived at an exterior angle of $136^{\circ}$ in cyclopropane, assuming a $\mathrm{C}-\mathrm{H}$ bond distance of $1.09 \AA$ and a C-C bond distance of $1.53 \AA$. However, it was later shown by Skinner (1947) that the moment of inertia determined by Smith is compatible with the model of Bastiensen \& Hassel.

The results of this work indicate that in 1,1,2,2tetramethylcyclopropane the average $\mathrm{C}-\mathrm{C}$ bond distance is $1.52 \pm 0.03 \AA$ and the external angle $\left(\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}\right)$ is $114 \pm 6^{\circ}$.

## Experimental

The sample of the compound used in this investigation was provided by Dr Greenlee of Ohio State University. It has an estimated purity of at least $98 \%$ and the following physical constants: b. p. $75 \cdot 89^{\circ} \mathrm{C}$. ( 760 mm .) ; $n^{20} D \quad 1.4009, d_{4}^{20} 0.7170 ;$ f. p. $-81 \cdot 05^{\circ}$ C.; $T_{f 0}$ (estimated by the 'midpoint' method) $-80.82^{\circ} \mathrm{C}$.

Electron-diffraction photographs were prepared in the customary manner (Brockway, 1936), using an apparatus built by Dr H.J. Yearian of the Purdue Physics Department. The camera distance was about 108 mm . and the electron wave-length about $0.055 \AA$. The recorded pattern extended to a $q$ of about 94 .

## Interpretation

The radial distribution method (Pauling \& Brockway, 1935; Shaffer, Schomaker \& Pauling, 1946) and the visual correlation method (Brockway, 1936; Pauling $\&$ Brockway, 1934) were used in the interpretation of the recorded pattern. The radial distribution function was calculated from the equation

$$
r D(r)=\sum_{q=1,2, \ldots}^{q \max } I(q) \exp \left(-b q^{2}\right) \sin \left(\frac{\pi}{10} q r\right)
$$

by the use of punched cards (Shaffer et al., 1946). The values of $I(q)$ were taken from the visual intensity curve (curve 'Vis', Fig. 2) which was drawn assuming no falling off of intensity with increasing $q$. The constant $b$ was chosen so that $\exp \left(-b q^{2}\right)=0.10$ at $q=100$.

The resulting curve (Fig. 2) shows two major peaks; the peak at $1.52 \AA$ corresponds to the average $\mathrm{C}-\mathrm{C}$ bond distance and the one at $2 \cdot 62 \AA$ to non-bonded $\mathrm{C}-\mathrm{C}$ distances of the type $\mathrm{C}_{4}-\mathrm{C}_{5}, \mathrm{C}_{4}-\mathrm{C}_{1}$ and $\mathrm{C}_{4}-\mathrm{C}_{3}$ (Fig. 1).

The peak at $1.08 \AA$ is in good agreement with the expected value for the $\mathrm{C}-\mathrm{H}$ bond but it is not as reliable as the other two peaks. The vertical lines


Fig. 1. Types of models constructed and parameter ranges studied.


Fig. 2. Radial distribution function and intensity curves.
beneath the curve correspond to the interatomic distances in one of the best models ( $L_{1.54}$ ) as determined by the correlation method.

The theoretical intensity curves were calculated from the expression

$$
I(q)=\sum_{i} \sum_{j} \frac{Z_{i} Z_{j}}{r_{i j}} \exp \left(-b_{i j} q^{2}\right) \sin \left(\frac{\pi}{10} q r_{i j}\right)
$$

The constant $b_{i j}$ in the exponential vibration factor was assigned the value 0.00018 for bonded $\mathrm{C}-\mathrm{H}$ terms, 0.0003 for non-bonded $\mathrm{C}-\mathrm{H}$ terms, and zero for all $\mathrm{C}-\mathrm{C}$ terms. All $\mathrm{H}-\mathrm{H}$ terms and all $\mathrm{C}-\mathrm{H}$ distances which change upon rotation of the side-chain methyl groups were not included in the calculations.

A few simplifying assumptions were made to reduce the number of structural parameters. The $\mathrm{C}-\mathrm{H}$ bond distances were taken to be $1.09 \AA$ and the $\mathrm{H}-\mathrm{C}-\mathrm{H}$ angles were assumed to be $109.5^{\circ}$. The $\mathrm{C}-\mathrm{C}$ bond distances in the ring were assumed equal and the side-chain carbon atoms were assumed to be symmetrically disposed so that the carbon skeleton has $C_{2 v}$ symmetry. The problem was thus reduced to one of four parameters, the following being chosen:
(1) the $\mathrm{C}-\mathrm{C}$ distance in the ring $\left(\mathrm{C}_{1}-\mathrm{C}_{2}\right)$, (2) the $\mathrm{C}-\mathrm{CH}_{3}$ distance $\left(\mathrm{C}_{2}-\mathrm{C}_{4}\right)$, (3) the external angle $(\angle X)$ and (4) the angle, measured in the plane of the ring, between a plane drawn through the $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}$ group and the $\mathrm{C}-\mathrm{C}$ bond direction in the ring $(\angle Y)$.

All models were calculated using a side-chain $\mathrm{C}-\mathrm{C}$ distance of $1.54 \AA$. The external angle, $X$, was varied from $106^{\circ}$ to $121^{\circ}$ in $3^{\circ}$ increments, and the angle $Y$
was varied from $160^{\circ}$ to $140^{\circ}$ ( $10^{\circ}$ on either side of the most symmetrical- $150^{\circ}$-arrangement in which the plane through the $\mathrm{CH}_{3}-\mathrm{C}_{-} \mathrm{CH}_{3}$ group bisects the angle of the ring) in $5^{\circ}$ increments. Values of the ring $\mathrm{C}-\mathrm{C}$ distance were chosen as $1.50,1.54$ and $1.58 \AA$. Models with ring C-C distances of $1 \cdot 42,1 \cdot 46,1 \cdot 62$ and $1.66 \AA$ were also calculated but only for more restricted ranges of the angular parameters, since these appeared incompatible with the radial distribution curve.
The representative curves shown in Fig. 2 are lettered according to the parameter chart in Fig. 1; the subscript denotes the ring C-C distance used in calculating the model. The change in the pattern with changes of the angular parameters for models with $\mathrm{C}-\mathrm{C}=1.54 \AA$ is representative of the change for other values of the ring C-C distance.

Curves for models $K_{1.54}, L_{1.54}, M_{1.54}, Q_{1.54}$ and $R_{1.54}$ are in good agreement with the visual curve. Curves $E_{1.54}, F_{1.54}$ and $G_{1.54}$ do not agree with the visual curve in that they show a doublet for the tenth maximum; these three curves were not rejected, however, owing largely to the fact that some allowance for vibration of the heavy atoms might well bring them into agreement. An attempt was made, in every case, to allow for such effects.

Models having an angle $Y$ of $160^{\circ}$ are illustrated by curve $A$; all were rejected on the basis of the appearance of the sixth and eighth maxima.

Curve $J$ is not acceptable because of wrong relative depths of the eighth and ninth minima; models $D$ and $O$ gave rise to curves showing even poorer agreement with the visual curve.
Curve $N$, typical of curves with angle $X$ greater than $118^{\circ}$, has the eighth minimum too deep relative to either the seventh or the ninth minima and was rejected on that basis.
Model $U$ is not acceptable since the curve does not show a peak corresponding to the eighth maximum; this is characteristic of models with $\angle Y=140^{\circ}$.

Curve $M X$ differs from curve $M$ in that it was obtained from a completely rigid molecule with no vibration factors for any of the terms. The difference between the two curves illustrates the qualitative effect of excluding $\mathrm{C}-\mathrm{H}$ terms which change upon rotation of the methyl groups and of placing vibration factors on the others; the quantitative effect is also very small.
Curves $K_{1.50}$ and $Q_{1.58}$ are typical of the best models obtained for the indicated ring C-C distances. The best models for ring C-C distances of $1.50 \AA$ and $1.58 \AA$ are in as good agreement with the visual curve as models with all C-C distances equal to $1 \cdot 54 \AA$.
For a ring C-C distance of $1.50 \AA$, acceptable models were obtained for values of angle $X$ from $109.5^{\circ}$ to $118^{\circ}$ and for values of $Y$ from $155^{\circ}$ to $145^{\circ}$. The best model is in the region of $K_{1.50}$. The region of acceptability for $\mathrm{C}-\mathrm{C}$ (ring) $=1.58 \AA$ extends from $X=$ $112^{\circ}$ to $118^{\circ}$ with $Y$ either $150^{\circ}$ or $145^{\circ}$. The best model is in the region of $Q_{1.55}$.

From these results it is concluded that the external angle (angle $X$ ) is $114 \pm 6^{\circ}$ and angle $Y$ is $150 \pm 8^{\circ}$. These values correspond to a C (ring)-C(ring) $-\mathrm{CH}_{3}$ angle of approximately $118^{\circ}$.

Table 1. Quantitative comparisons for model $L_{1.54}$

| Maximum | Minimum | $q_{0}$ | $q / q_{0}\left(L_{1.54}\right)$ |
| :---: | :---: | :---: | :---: |
|  | 2 | 13.59 | (0.934) |
| 2 |  | 16.96 | 0.996 |
|  | 3 | $22 \cdot 15$ | 0.952 |
| 3 |  | $25 \cdot 18$ | 0.997 |
|  | 4 | $28 \cdot 49$ | 0.972 |
| 4 |  | 31.64 | 0.967 |
|  | 5 | 36.67 | 0.974 |
| 5 |  | $40 \cdot 68$ | 1.003 |
|  | 6 | 44.60 | 0.998 |
| 6 |  | $47 \cdot 23$ | 0.991 |
|  | 7 | $5 \mathrm{l} \cdot 30$ | 0.980 |
| 7 |  | 55.57 | 0.999 |
|  | 8 | 60.00 | 1.001 |
| 8 |  | 63.30 | 0.995 |
|  | 9 | 65.95 | 0.993 |
| 9 |  | $70 \cdot 09$ | 0.990 |
|  | 10 | 74.80 | 0.990 |
| 10 |  | 81.07 | - |
|  | 11 | 89.06 | 1.000 |
| 11 |  | $94 \cdot 00$ | 0.992 |
|  |  | Mean | 0.988 |
|  |  | Mean dev. | 0.011 |

Quantitative comparisons for one of the best models are given in Table 1. A consideration of all the acceptable models shows that the range of ring $\mathrm{C}-\mathrm{C}$ distances is greater than the range of side-chain $\mathrm{C}-\mathrm{C}$ distances, and hence the latter is determined with more precision. The final bond distances are:

$$
\begin{aligned}
& \mathrm{C}-\mathrm{C}(\text { ring })=1.52+b \pm 0 \cdot 04 \AA \\
& \mathrm{C}-\mathrm{C}(\text { side-chain })=1.52-b,
\end{aligned}
$$

where $-0.04 \leq b \leq 0.04$. The average $\mathrm{C}-\mathrm{C}$ distance is more accurately determined as $1.52 \pm 0.03 \AA$. Comparison of the final distances in model $L_{1.54}$ is made with the radial distribution curve in Fig. 2.

## Discussion

The results obtained in this investigation are in fairly good agreement with the results of studies on other cyclopropane derivatives to which reference has been made in the introduction. The best value for the external angle ( $114^{\circ}$ ) found in this study is smaller than the value of $118 \cdot 2^{\circ}$ found by Bastiansen \& Hassel (1946) in cyclopropane, although it is impossible to exclude tetramethylcyclopropane models having values of this angle as large as $120^{\circ}$. An external bond angle of $114^{\circ}$ does not confirm values of $120^{\circ}$ (Walsh, 1949) and $122^{\circ}$ (Kilpatrick \& Spitzer, 1946) proposed on the basis of bond-orbital theories. It agrees well, however, with the value of $113^{\circ}$ calculated by Coulson \& Moffitt (1947) who introduced somewhat different assumptions into the bond-orbital method.

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# The Crystal Structure of $\boldsymbol{m}$-Tolidine 

By F. Fowweather<br>Physics Department, College of Technology, Manchester 1, England

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Standard single-crystal methods show that the unit cell of $m$-tolidine is orthorhombic, with $a=7 \cdot 60, b=14.81, c=21 \cdot 05 \AA$; the cell contains eight molecules and has space group Pcab. The atomic co-ordinates are obtained by two-dimensional Fourier methods, together with the methods of steepest descents and error syntheses.

The two phenyl rings in each molecule are mutually inclined at an angle of $86^{\circ}$. The diphenyl link is $1.55 \AA$ and the C-C bonds vary considerably with values between 1.31 and $1.41 \AA$. The structure is racemic with four right-handed and four left-handed molecules in the unit cell.

## Introduction

The work described is a contribution to a survey of a number of substituted diphenyls; a preliminary

(I)

(II)

(III)
account of the survey has been given by Hargreaves \& Taylor (1941). The structure of $m$-tolidine dihydro-
chloride (I) was determined by Hargreaves (1940) and refined by Fowweather \& Hargreaves (1950). Smare (1948) determined the structure of $2-2^{\prime}$ dichlorobenzidine (II).

## Physical and X-ray data

$m$-Tolidine (III) is difficult to crystallize and forms soft, transparent rectangular plates, which cleave easily only parallel to the edge [010] of the plate face (001). The melting point is $89-90^{\circ} \mathrm{C}$.

X-ray rotation, oscillation and Weissenberg photographs show that the crystals are orthorhombic with axial lengths
$a=7 \cdot 60 \pm 0 \cdot 03, b=14 \cdot 81 \pm 0.06$ and $c=21 \cdot 05 \pm 0 \cdot 1 \AA$.
The density measured by flotation in a mixture of chloroform and alcohol is $1 \cdot 18 \pm 0.01 \mathrm{~g} . \mathrm{cm} .^{-3}$. There are eight molecules per unit-cell, giving a calculated density of $1.182 \mathrm{~g} . \mathrm{cm} .^{-3}$.

Absent spectra determine the space group to be Pcab-D ${ }_{2 h}^{15}$.

Zero-layer-line Weissenberg photographs were taken with $\mathrm{Cu} K \alpha$ radiation, the crystal being rotated about the $a$ and $b$ axes. It was difficult to cut the soft crystals, and in addition the plates were thin, with a thickness


[^0]:    * From the Ph.D. Thesis of H. P. Lemaire, Research Corporation Fellow in Chemistry, Purdue University, 1949-50.
    $\dagger$ Present address: Department of Chemistry, St. Michael's College, Winooski Park, Vermont, U.S.A.

